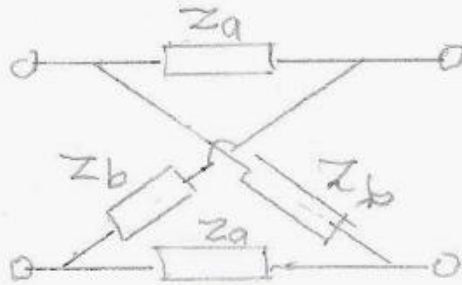


# HOMWORK 1

ECE 580, 2022

## Solutions

1. Find the ABCD parameters of the symmetrical lattice shown.



Easy way: go through z parameters. By inspection,

$$Z_{11} = Z_{22} = (Z_a + Z_b)/2$$

$$Z_{12} = Z_{21} = (Z_b - Z_a)/2$$

From the Table on p. 42,

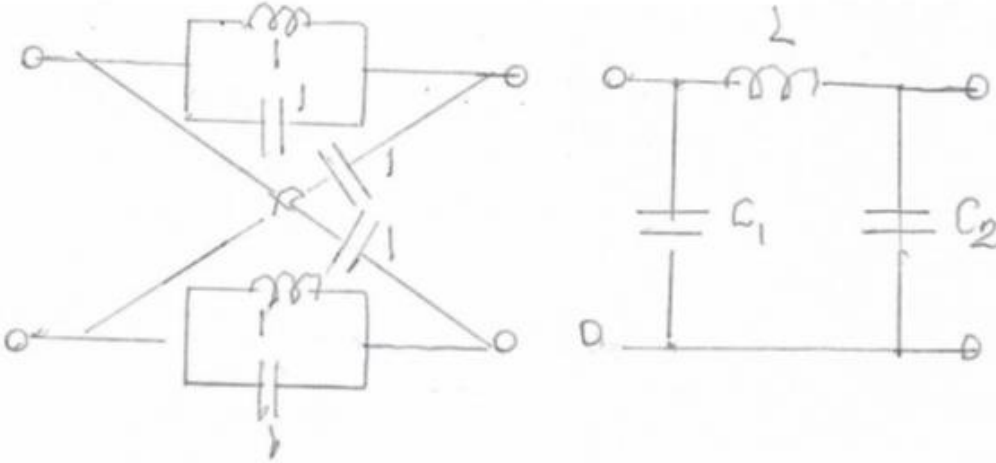
$$A = D = Z_{11}/Z_{12} = (Z_a + Z_b)/(Z_b - Z_a)$$

$$B = |Z|/Z_{12} = 2 Z_a Z_b/(Z_b - Z_a)$$

$$C = 1/Z_{12} = 2/(Z_b - Z_a)$$

As a check,  $A \cdot D - B \cdot C = 1$ . Reciprocal two-port!

2. The two two-ports shown below are equivalent. Find the element values of the ladder circuit.



Using the equations of Problem 1,

$$Z_{11} = Z_{22} = (Z_a + Z_b)/2 = (2s^2 + 1)/(2s^3 + 2s)$$

$$Z_{12} = Z_{21} = (Z_b - Z_a)/2 = 1/(2s^3 + 2s)$$

For the ladder,

$$Z_{11} = (LC_2s^2 + 1) / [ LC_1C_2s^3 + (C_1+C_2)s]$$

Equating coefficients of powers of  $s$  gives

$$C_1 = C_2 = 1$$

$$L = 2.$$